

Fractals

The second minor project is the generation of a fractal following the chaos game and algorithm describe in the research paper “The Fractal Flame Algorithm” From Scott Draves and Erik Reckase.

First, we have a set of linear or no linear function which applies a simple transformation on a point. For each function, we defined also six parameters a_x, b_x, c_x and a_y, b_y, c_y and a probability value. Then, the following algorithm is executed:

```
float x,y;
x=y=0;
For each n iterations (number of vertices)
    Select randomly a function (with probability)
    x=xax+ ybx+ cx
    y=xay+ yby+ cy
    Call Function no linear on (x,y)
    Draw a pixel in x,y
```

In this project, we have two functions “spherical” with different parameter; the probability of execution of each function is the same. The spherical function is described by this relation.

$$\begin{cases} x = \frac{x}{x^2 + y^2} \\ y = \frac{y}{x^2 + y^2} \end{cases} \text{ and } x^2 + y^2 \neq 0$$

The two functions have two colours, the green and the red, the hue value is interpolated for each draw thanks to a representation of the colours in HSL space. It is possible to use a palette to modify this interpolation and give a different result.

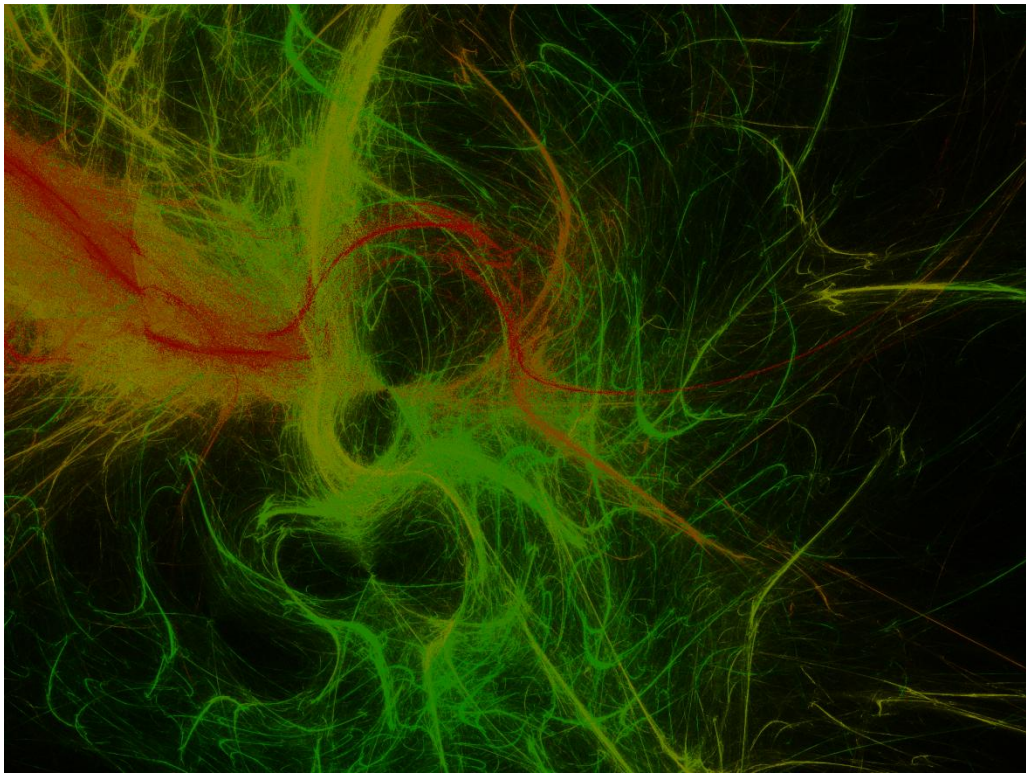


Figure 1: Fractal without palette

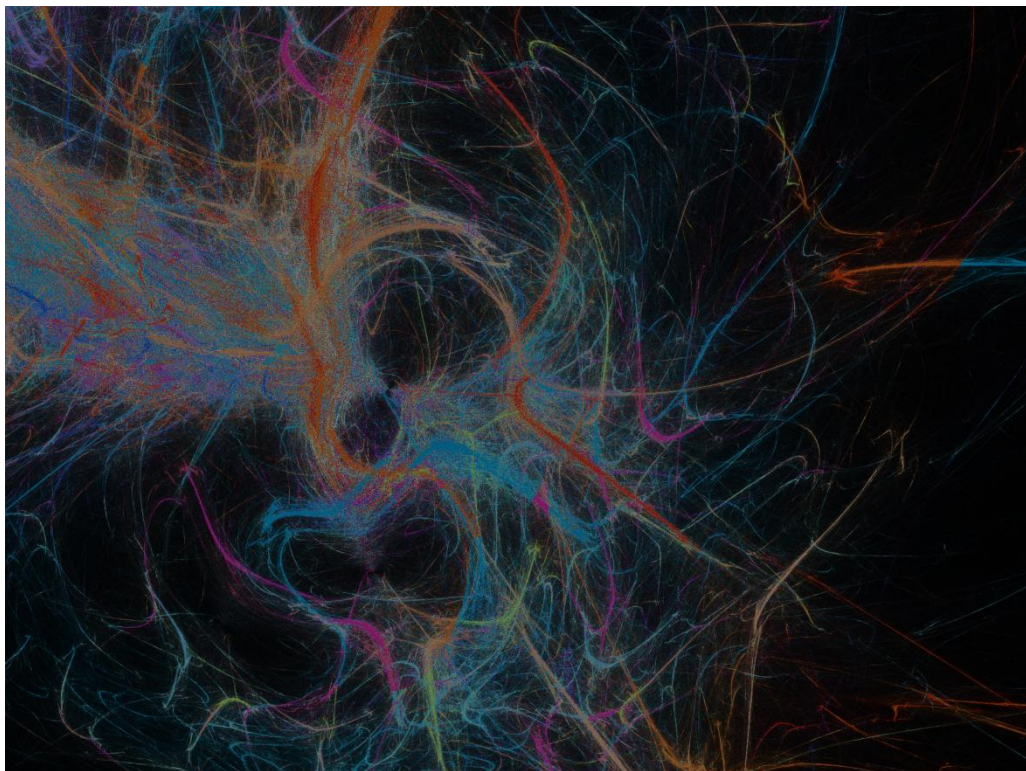


Figure 2: Fractal with a defined palette

It is interesting to see that it is always possible to generate the triangle of Sierpinski with a particular set of functions, The linear parameter are set to ignore this transformation ($x=x$ and $y=y$) :

$$\begin{cases} x = \frac{x}{2} \\ y = \frac{y}{2} \end{cases} \quad \begin{cases} x = \frac{x+1}{2} \\ y = \frac{y}{2} \end{cases} \quad \begin{cases} x = \frac{x}{2} \\ y = \frac{y+1}{2} \end{cases}$$

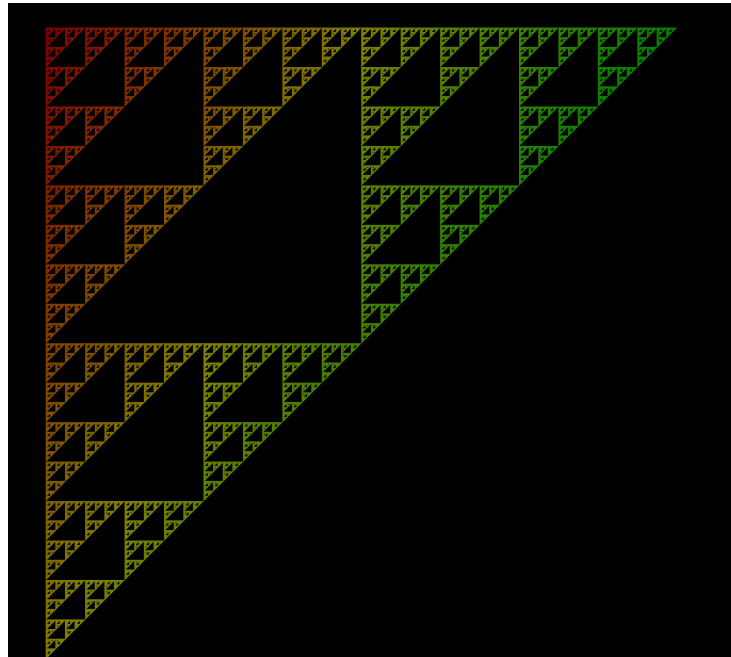


Figure 3: Triangle of Sierpinski

The animation of the fractal is done modifying randomly values of the six linear parameters, each frame is saved into a BMP file and a video is created from this list of images (see “**Animated Fractal.avi**”).